

# Excited baryons in the large $N_c$ limit

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# Motivation

- Traditional issues to study **baryons**: **effective theories** and **constituent quark models**
- The  $1/N_c$  expansion is a **new theoretical method** (1993)
  - Systematic
  - Valid for the whole energy region
  - Model independent
  - Predictive
  - Gives support to constituent quark models
  - Used to study baryon masses, magnetic moments, axial currents, decay widths

# Large $N_c$ QCD

- 't Hooft suggested to **generalize QCD** to  $N_c$  colors [1] in the limit  $\frac{g}{\sqrt{N_c}} \rightarrow 0$ ,  $g$  fixed when  $N_c \rightarrow \infty$

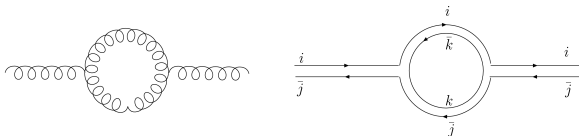


Diagram of order  $\mathcal{O}(1)$

- Witten : Large  $N_c$  power counting rules for Feynman diagrams [2]**  
The leading Feynman diagrams are planar and contain a minimum number of quark loops

[1] G. 't Hooft, Nucl. Phys. **72**, 461 (1974).

[2] E. Witten, Nucl. Phys. **B160**, 57 (1979).

## Mesons in large $N_c$ QCD

$$|1\rangle_c = \frac{1}{\sqrt{N_c}} \underbrace{(\bar{l}l + \bar{m}m + \dots + \bar{n}n)}_{N_c \text{ terms}}$$

Large  $N_c$  mesons are stable and non-interacting

## Baryons in large $N_c$ QCD

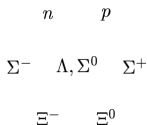
$$\varepsilon_{i_1 i_2 i_3 \dots i_{N_c}} q^{i_1} q^{i_2} q^{i_3} \dots q^{i_{N_c}}$$

bound states of  $N_c$  **valence quarks completely antisymmetric in color**  
because baryons are colorless

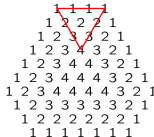
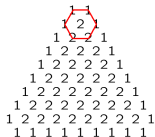
**Baryon mass grows with  $N_c$**

## Baryon weight diagrams

For  $N_c = 3$



For large  $N_c$



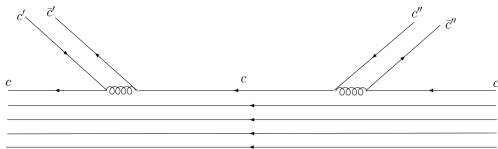
Familiar  $N_c = 3$  baryons can be **identified** with **states at the top of the flavor representations**

**Exact  $SU_f(3)$**  : all particles in **each weight diagram** have the **same mass** when  $m_u = m_d = m_s$

**Exact  $SU(6)$**  : **all the particles** have the **same mass**

## Baryon-meson scattering amplitude

baryon + meson  $\rightarrow$  baryon + meson  $\sim \mathcal{O}(1)$



$$[X_0^{ia}, X_0^{jb}] = 0, \text{ consistency condition for unitarity}$$

$\Rightarrow$  **SU(2N<sub>f</sub>) contracted is an exact symmetry in  $N_c \rightarrow \infty$  limit [3,4]**

$\Rightarrow$  **Infinite tower of degenerate baryon states**

SU(2N<sub>f</sub>)<sub>c</sub> symmetry realized at  $N_c \rightarrow \infty$  by **Skyrme model** and **non-relativistic quark model**

[3] J.-L. Gervais and B. Sakita, Phys. Rev. Lett. **52**, 87 (1984); Phys. Rev. **D30**, 1795 (1984).

[4] R. Dashen and A. V. Manohar, Phys. Lett. **B315**, 425 (1993).

SU(6) symmetry of non-relativistic quark model **exact in the large  $N_c$  limit** for ground state baryons

**Assumed SU(6)  $\times$  O(3) for excited states** to include  $\ell \neq 0$

**SU( $2N_f$ ) generators**

$$S^i = q^\dagger (S^i \otimes \mathbb{1}) q \quad (3, 1)$$

$$T^a = q^\dagger (\mathbb{1} \otimes T^a) q \quad (1, \text{adj})$$

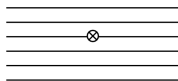
$$G^{ia} = q^\dagger (S^i \otimes T^a) q \quad (3, \text{adj})$$

**SO(3) generators (excited states)**

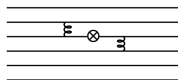
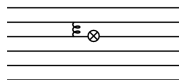
$$\ell^i = q^\dagger \ell^i q \quad (3)$$



## $1/N_c$ Expansion of a QCD 1-body operator [5]



(a)



(b)

$1/N_c$  expansion of a static QCD 1-body operator (baryon mass, axial vector current, magnetic moment) transforming according to a given  $SU(2) \times SU(N_f)$  representation

$$\mathcal{O}_{\text{QCD}}^{1\text{-body}} = \sum_n \frac{1}{N_c^{n-1}} c_n O^n, \quad O^n = O_\ell \cdot O_{SF}$$

where  $O_\ell$  and  $O_{SF}$  are expressed in terms of products of  $SO(3)$  and  $SU(2N_f)$  generators

[5] R. Dashen, E. Jenkins and A. V. Manohar, Phys. Rev. **D51**, 3697 (1995).

# The Baryon Structure

The **total wave function of baryons**  $\Psi$

$$\Psi = \psi_{lm} \chi \phi C$$

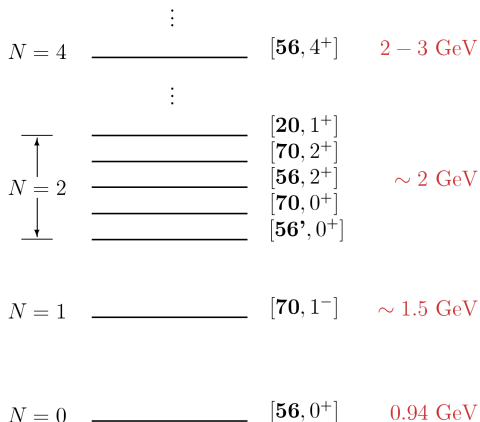
$\psi_{lm}$ ,  $\chi$ ,  $\phi$  and  $C$  are the orbital, spin, flavor and color parts

**Steps in forming  $SU(6) \times O(3)$  symmetric wave functions** for low excitations and  $N_c = 3$

SU(3)		SU(2)	SU(6)		O(3)	SU(6) $\times$ O(3)
10	$\times$	$\frac{3}{2}$	56	$\times$	$2_2^+ S$	<b>[56, 2<sup>+</sup>]</b>
8	$\times$	$\frac{1}{2}$		$\times$	$0_2^+ S$	<b>[56', 0<sup>+</sup>]</b>
					$0_0^+ S$	<b>[56, 0<sup>+</sup>]</b>
10	$\times$	$\frac{1}{2}$	70	$\times$	$2_2^+ M$	<b>[70, 2<sup>+</sup>]</b>
8	$\times$	$\frac{3}{2}$		$\times$	$0_2^+ M$	<b>[70, 0<sup>+</sup>]</b>
8	$\times$	$\frac{1}{2}$		$\times$	$1_1^- M$	<b>[70, 1<sup>-</sup>]</b>
1	$\times$	$\frac{1}{2}$				
8	$\times$	$\frac{1}{2}$	20	$\times$	$1_2^+ A$	<b>[20, 1<sup>+</sup>]</b>
1	$\times$	$\frac{3}{2}$				

## Baryon spectrum

SU(6) notation:  $[\mathbf{X}, l^P]$ ,  $N_c = 3$



# Excited States I

## First approach [6]

- Witten's suggestion: **Hartree approximation in  $N_c \rightarrow \infty$  limit**
  - Each quark moves in an **average potential** generated by the other  $N_c - 1$  quarks
  - Total potential experienced by **each quark** is of order  $\mathcal{O}(1)$
  - Interaction between **any given pair of quarks** of order  $\mathcal{O}(1/N_c)$
- Low excitations: baryons composed of  $\mathcal{O}(N_c)$  **ground-state quarks** (the core) and  $\mathcal{O}(1)$  **excited quarks**
- The core quarks are described by **symmetric wave functions in both orbital and spin-flavor parts** as ground-state baryons
- **Excited quark** coupled to **a symmetric ground state core**

[6] J.L. Goity, Phys. Lett. **B414**, 140 (1997).

Extensively applied to  $[70, 1^-]$  baryon :

ground state core made of  $N_c - 1$  quarks + one excited quark (2 flavors [7], 3 flavors [8])

$$S^i = s^i + S_c^i; \quad T^a = t^a + T_c^a; \quad G^{ia} = g^{ia} + G_c^{ia}$$

Wave function :

$$\begin{aligned} |\ell S; JJ_3; (\lambda\mu)YII_3\rangle &= \sum_{\substack{m_\ell, S_3, m_1, m_2, \\ Y_c, I_c, I_{c3}, y, i, i_3}} \left( \begin{array}{cc|c} \ell & S & J \\ m & S_3 & J_3 \end{array} \right) \\ &\times \sum_{pp'} c_{pp'}^{[N_c-1,1]}(S) \left( \begin{array}{cc|c} S_c & \frac{1}{2} & S \\ m_1 & m_2 & S_3 \end{array} \right) \left( \begin{array}{cc|c} (\lambda_c\mu_c) & (10) & (\lambda\mu) \\ Y_c I_c I_{c3} & y i i_3 & Y I I_3 \end{array} \right) \\ &\times |S_c m_1\rangle |1/2 m_2\rangle |(\lambda_c\mu_c) Y_c I_c I_{c3}\rangle |(10) y i i_3\rangle |\ell m\rangle \end{aligned}$$

$c_{pp'}^{[N_c-1,1]}(S)$  are isoscalar factors of  $S_{N_c}$

[7] C.E. Carlson, C.D. Carone, J.L. Goity and R.F. Lebed, Phys. Rev. **D59**, 114008 (1999).

[8] J.L. Goity, C.L. Schat and N.N. Scoccola, Phys. Rev. **D66**, 114014 (2002).

Has also been applied to  $[\mathbf{70}, \ell^+]$  ( $\ell = 0, 2$ ) [9]

## Mass operator

$$M_{[\mathbf{70}, \ell^+]} = \sum_{i=1}^6 c_i O_i + \sum_{j=1}^4 d_j B_j$$

Operator	Fitted coef. (MeV)
$O_1 = N_c \mathbb{1}$	$c_1 = 556 \pm 11$
$O_2 = \ell_q^i s^i$	$c_2 = -43 \pm 47$
$O_3 = \frac{3}{N_c} \ell_q^{(2)ij} g^{ia} G_c^{ja}$	$c_3 = -85 \pm 72$
$O_4 = \frac{4}{N_c+1} \ell^i t^a G_c^{ia}$	
$O_5 = \frac{1}{N_c} (S_c^i S_c^i + s^i S_c^i)$	$c_5 = 253 \pm 57$
$O_6 = \frac{1}{N_c} t^a T_c^a$	$c_6 = -25 \pm 86$
$B_1 = t^8 - \frac{1}{2\sqrt{3}N_c} O_1$	$d_1 = 365 \pm 169$
$B_2 = T_c^8 - \frac{N_c-1}{2\sqrt{3}N_c} O_1$	$d_2 = -293 \pm 54$
$B_4 = 3\ell_q^i g^{i8} - \frac{\sqrt{3}}{2} O_2$	

$$\chi_{\text{dof}}^2 = 1.0$$

[9] N. Matagne and Fl. Stancu, Phys. Rev. **D74**, 034014 (2006)

## [70, 1<sup>-</sup>] non-strange baryons : the three towers of states [10], [11]

For  $N_c \geq 5, I \leq 3/2$ , 13 states :

$$N_{1/2}, N'_{1/2}, N_{3/2}, N'_{3/2}, N_{5/2}, \Delta_{1/2}, \Delta'_{1/2}, \Delta_{3/2}, \Delta'_{3/2}, \Delta''_{3/2}, \Delta'_{5/2}, \Delta''_{5/2}, \Delta''_{7/2}$$

Considering  $H$  of order up to  $\mathcal{O}(N_c^0)$ ,

$$H = c_1 N_c + c_2 \ell \cdot s + \frac{1}{N_c} \ell^{(2)} \cdot g \cdot G_c$$

Diagonalize it in the basis of the 13 states

⇒ **Observe a pattern of degeneracy**

$$\begin{aligned} & N_{1/2}, \Delta_{3/2} \quad (m_0) \\ & N'_{1/2}, \Delta_{1/2}, N_{3/2}, \Delta'_{3/2}, \Delta_{5/2} \quad (m_1) \\ & \Delta'_{1/2}, N'_{3/2}, \Delta''_{3/2}, N_{5/2}, \Delta'_{5/2}, \Delta''_{7/2} \quad (m_2) \end{aligned}$$

according to  $|I - J| \leq K$

[10] T. Cohen and R.F. Lebed, Phys. Rev. **D67**, 096008 (2003).

[11] D. Pirjol and C. Schat, Phys. Rev. **D67**, 096009 (2003).

# Excited States II

## Second approach

- A totally symmetric orbital-spin-flavor state

$$\Phi_S = \frac{1}{\sqrt{N_c - 1}} \sum_Y |[N_c - 1, 1]Y\rangle_O |[N_c - 1, 1]Y\rangle_{SF}$$

Illustration for  $N_c = 5$  ( $[70, 1^-]$ )

$$\boxed{1\ 2\ 3\ 4\ 5} = \frac{1}{\sqrt{4}} \left( \begin{array}{c} \boxed{1\ 2\ 3\ 4} \\ \boxed{5} \end{array} + \begin{array}{c} \boxed{1\ 2\ 3\ 4} \\ \boxed{5} \end{array} + \begin{array}{c} \boxed{1\ 2\ 3\ 5} \\ \boxed{4} \end{array} + \begin{array}{c} \boxed{1\ 2\ 3\ 5} \\ \boxed{4} \end{array} \right. \\ \left. + \begin{array}{c} \boxed{1\ 2\ 4\ 5} \\ \boxed{3} \end{array} + \begin{array}{c} \boxed{1\ 2\ 4\ 5} \\ \boxed{3} \end{array} + \begin{array}{c} \boxed{1\ 3\ 4\ 5} \\ \boxed{2} \end{array} + \begin{array}{c} \boxed{1\ 3\ 4\ 5} \\ \boxed{2} \end{array} \right)$$

Young tableau	Young-Yamanouchi basis vectors of [41]
$\begin{array}{c} \boxed{1\ 2\ 3\ 4} \\ \boxed{5} \end{array}$	$\frac{1}{\sqrt{20}} (4ssssp - sssps - sspss - spsss - pssss)$
$\begin{array}{c} \boxed{1\ 2\ 3\ 5} \\ \boxed{4} \end{array}$	$\frac{1}{\sqrt{12}} (3ssps - spss - spsss - pssss)$
$\begin{array}{c} \boxed{1\ 2\ 4\ 5} \\ \boxed{3} \end{array}$	$\frac{1}{\sqrt{6}} (2ssps - spss - pssss)$
$\begin{array}{c} \boxed{1\ 3\ 4\ 5} \\ \boxed{2} \end{array}$	$\frac{1}{\sqrt{2}} (spss - pssss)$

- As  $S_c = I_c$ , in the decoupling picture, information on isospin is lost



## Matrix elements of the spin-spin and isospin-isospin operators with the exact and the approximate wave function

	$\langle s \cdot S_c \rangle$		$\langle S_c^2 \rangle$	
	approx. w.f.	exact w.f.	approx. w.f.	exact w.f.
$^2_8$	$-\frac{N_c+3}{4N_c}$	$-\frac{3(N_c-1)}{4N_c}$	$\frac{N_c+3}{2N_c}$	$\frac{3(N_c-1)}{2N_c}$
$^4_8$	$\frac{1}{2}$	$-\frac{3(N_c-5)}{4N_c}$	2	$\frac{3(3N_c-5)}{2N_c}$
$^2_{10}$	-1	$-\frac{3(N_c-1)}{4N_c}$	2	$\frac{3(N_c-1)}{2N_c}$

	$\langle t \cdot T_c \rangle$		$\langle T_c^2 \rangle$	
	approx. w.f.	exact w.f.	approx. w.f.	exact w.f.
$^2_8$	$-\frac{N_c+3}{4N_c}$	$-\frac{3(N_c-1)}{4N_c}$	$\frac{N_c+3}{2N_c}$	$\frac{3(N_c-1)}{2N_c}$
$^4_8$	-1	$-\frac{3(N_c-1)}{4N_c}$	2	$\frac{3(N_c-1)}{2N_c}$
$^2_{10}$	$\frac{1}{2}$	$-\frac{3(N_c-5)}{4N_c}$	2	$\frac{3(3N_c-5)}{2N_c}$

## Results of the fits (nonstrange baryons)

- Only with the **7 resonances**:  ${}^2N_{1/2}(1538 \pm 18)$ ,  ${}^4N_{1/2}(1660 \pm 20)$ ,  ${}^2N_{3/2}(1523 \pm 8)$ ,  ${}^4N_{3/2}(1700 \pm 50)$ ,  ${}^4N_{5/2}(1678 \pm 8)$ ,  ${}^2\Delta_{1/2}(1645 \pm 30)$  and  ${}^2\Delta_{3/2}(1720 \pm 50)$

### Fit 1

Operator		Approx. w.f. (MeV)	Exact w.f. (MeV)
$O_1 = N_c \mathbb{1}$	$c_1 =$	$211 \pm 23$	$299 \pm 20$
$O_2 = \ell^i s^i$	$c_2 =$	$3 \pm 15$	$3 \pm 15$
$O_3 = \frac{1}{N_c} s^i S_c^i$	$c_3 =$	$-1486 \pm 141$	$-1096 \pm 125$
$O_4 = \frac{1}{N_c} S_c^i S_c^i$	$c_4 =$	$1182 \pm 74$	$1545 \pm 122$
$O_5 = \frac{1}{N_c} t^a T_c^a$	$c_5 =$	$-1508 \pm 149$	$417 \pm 79$
$\chi_{\text{dof}}^2$		1.56	1.56

## Fit 2

Operator		Approx. w.f. (MeV)	Exact w.f. (MeV)
$O_1 = N_c \mathbb{1}$	$c_1 =$	$484 \pm 4$	$484 \pm 4$
$O_2 = \ell^i s^i$	$c_2 =$	$3 \pm 15$	$3 \pm 15$
$O'_3 = \frac{1}{N_c} (2s^i S_c^i + S_c^i S_c^i + \frac{3}{4})$	$c'_3 =$	$150 \pm 11$	$150 \pm 11$
$O'_5 = \frac{1}{N_c} (2t^a T_c^a + T_c^a T_c^a + \frac{3}{4})$	$c'_5 =$	$139 \pm 27$	$139 \pm 27$
$\chi_{\text{dof}}^2$		1.04	1.04

⇒ **No decoupling of the wave function and the operators**

$S^i, T^a, G^{ia}$

**Wave function [12]**

$$|\ell S(\lambda\mu)YII_3; JJ_3\rangle = \sum_{m_\ell, S_3} \left( \begin{array}{cc|c} \ell & S & J \\ m_\ell & S_3 & J_3 \end{array} \right) |[N_c-1, 1]SS_3(\lambda\mu)YII_3] |[N_c-1, 1]\ell m_\ell\rangle$$

**Generators : Wigner-Eckart theorem for SU(6)**

$$\begin{aligned} &\langle [N_c-1, 1](\lambda'\mu')Y'I'I'_3S'S'_3|E^{ia}|[N_c-1, 1](\lambda\mu)YII_3SS_3\rangle = \\ &\sqrt{C^{[N_c-1, 1]}(\text{SU}(6))} \left( \begin{array}{cc|c} S & S^i & S' \\ S_3 & S_3^i & S'_3 \end{array} \right) \left( \begin{array}{cc|c} I & I^a & I' \\ I_3 & I_3^a & I'_3 \end{array} \right) \\ &\times \sum_{\rho=1,2} \left( \begin{array}{cc|c} (\lambda\mu) & (\lambda^a\mu^a) & \\ YI & Y^aI^a & \\ \hline (\lambda'\mu') & & \\ Y'I' & & \end{array} \right)_\rho \left( \begin{array}{cc|c} [N_c-1, 1] & [21^4] & [N_c-1, 1] \\ (\lambda\mu)S & (\lambda^a\mu^a)S^i & (\lambda'\mu')S' \end{array} \right)_\rho \end{aligned}$$

where  $C^{[N_c-1, 1]}(\text{SU}(6)) = N_c(5N_c + 18)/12$  is the SU(6) Casimir operator for irrep  $[N_c - 1, 1]$

$$E^i = \frac{S^i}{\sqrt{3}}; \quad E^a = \frac{T^a}{\sqrt{2}}; \quad E^{ia} = \sqrt{2}G^{ia}$$

[12] N. Matagne and F.L. Stancu, Phys. Rev. **D83**, 056007 (2011).

Isoscalar factors for the  $48$  states

$(\lambda_1 \mu_1) S_1$	$(\lambda_2 \mu_2) S_2$	$\rho$	$\left( \begin{array}{cc c} [N_c - 1, 1] & [21^4] & [N_c - 1, 1] \\ (\lambda_1 \mu_1) S_1 & (\lambda_2 \mu_2) S_2 & (\lambda - 2, \mu + 1) S \end{array} \right)_\rho$
$(\lambda - 2, \mu + 1) S$	(11)1	1	$[N_c(4S - 3) + 6S] \sqrt{\frac{2(S+1)}{S[N_c(N_c+6)+12(S-1)S]N_c(5N_c+18)}}$
$(\lambda - 2, \mu + 1) S$	(11)1	2	$-\frac{N_c - 2S}{S} \sqrt{\frac{3(S-1)(S+1)(N_c - 2S + 6)(N_c + 2S)(N_c + 2S + 4)}{2(N_c - 2S + 2)[N_c(N_c + 6) + 12(S-1)S]N_c(5N_c + 18)}}$
$(\lambda \mu) S + 1$	(11)1	/	$-\sqrt{\frac{3}{2}} \sqrt{\frac{2S+3}{2S+1}} \sqrt{\frac{(N_c - 2S)(N_c + 2S + 4)}{N_c(5N_c + 18)}}$
$(\lambda \mu) S$	(11)1	/	$-\frac{1}{S} \sqrt{\frac{3}{2}} \sqrt{\frac{(N_c - 2S)(N_c + 2S + 4)}{(N_c + 2S + 2)(5N_c + 18)}}$
$(\lambda \mu) S - 1$	(11)1	/	$\frac{N_c + 4S^2}{S} \sqrt{\frac{3(N_c + 2S + 4)}{2(2S - 1)(2S + 1)(N_c + 2S + 2)N_c(5N_c + 18)}}$
$(\lambda - 2, \mu + 1) S - 1$	(11)1	1	$\frac{3\sqrt{2(S-1)(N_c+2S)}}{\sqrt{S[N_c(N_c+6)+12(S-1)S](5N_c+18)}}$
$(\lambda - 2, \mu + 1) S - 1$	(11)1	2	$-\frac{N_c}{S} \sqrt{\frac{3(N_c - 2S + 6)(N_c + 2S + 4)}{2(N_c - 2S + 2)[N_c(N_c + 6) + 12(S-1)S](5N_c + 18)}}$
$(\lambda - 1, \mu - 1) S$	(11)1	/	$-2\sqrt{\frac{3(S+1)(N_c - 2S)(N_c + 2S)}{S(N_c - 2S + 2)(N_c + 2S + 2)N_c(5N_c + 18)}}$
$(\lambda - 1, \mu - 1) S - 1$	(11)1	/	$2(S - 1) \sqrt{\frac{3(N_c - 2S)(N_c + 2S)}{S(2S - 1)(N_c - 2S + 2)(N_c + 2S + 2)N_c(5N_c + 18)}}$
$(\lambda - 3, \mu) S - 1$	(11)1	/	$-2\sqrt{\frac{3(S-1)(N_c+2S-2)}{(2S-1)(N_c-2S+4)N_c(5N_c+18)}}$
$(\lambda - 4, \mu + 2) S - 1$	(11)1	/	$-\sqrt{\frac{3}{2}} \sqrt{\frac{2S-3}{2S-1}} \sqrt{\frac{(N_c+2S)(N_c-2S+2)(N_c-2S+6)}{(N_c-2S+4)N_c(5N_c+18)}}$
$(\lambda - 2, \mu + 1) S$	(11)0	1	$\sqrt{\frac{N_c(N_c+6)+12(S-1)S}{2N_c(5N_c+18)}}$
$(\lambda - 2, \mu + 1) S$	(11)0	2	0
$(\lambda - 2, \mu + 1) S$	(00)1	/	$\sqrt{\frac{4S(S+1)}{N_c(5N_c+18)}}$

$$M_{[\mathbf{70}, 1^-]} = \sum_i c_i O_i + \sum_j d_j B_j$$

Operator	Fit 1 (MeV)	Fit 2 (MeV)	Fit 3 (MeV)
$O_1 = N_c \mathbb{1}$	$489 \pm 4$	$492 \pm 4$	$492 \pm 4$
$O_2 = \ell^i s^i$	$24 \pm 6$	$6 \pm 6$	$6 \pm 5$
$O_3 = \frac{1}{N_c} S^i S^i$	$129 \pm 10$	$123 \pm 10$	$123 \pm 10$
$O_4 = \frac{1}{N_c} [T^a T^a - \frac{1}{12} N_c (N_c + 6)]$	$145 \pm 16$	$134 \pm 16$	$135 \pm 16$
$O_5 = \frac{3}{N_c} L^i T^a G^{ia}$	$-19 \pm 7$	$3 \pm 7$	$4 \pm 3$
$O_6 = \frac{15}{N_c} L^{(2)ij} G^{ia} G^{ja}$	$9 \pm 1$	$9 \pm 1$	$9 \pm 1$
$O_7 = \frac{1}{N_c^2} L^i G^{ja} \{S^j, G^{ia}\}$	$129 \pm 33$	$6 \pm 33$	
$B_1 = -S$	$138 \pm 8$	$138 \pm 8$	$137 \pm 8$
$B_2 = \frac{1}{N_c} \sum_{i=1}^3 T^i T^i - O_4$	$-59 \pm 18$	$-40 \pm 18$	$-40 \pm 18$
$\chi_{\text{dof}}^2$	1.7	0.9	0.84

- **Fit 1** :  $M(\Lambda(1405)) = 1407$  MeV
- **Fit 2-3** :  $M(\Lambda(1405)) = 1500$  MeV
- Important role of  $O_7$  in Fit 1 ( $\chi_{\text{dof}}^2 = 2.95$  without it)
- $O_2$  and  $O_7$  contribute to the  $\Lambda(1405) - \Lambda(1520)$  splitting
- **Spin operator**  $O_3$  dominant for  $N$
- **Flavor operator**  $O_4$  dominant for  $\Delta$

## Results for Fit 1

	Part. contrib. (MeV)										Total (MeV)	Exp. (MeV)	Name, status
	$c_1O_1$	$c_2O_2$	$c_3O_3$	$c_4O_4$	$c_5O_5$	$c_6O_6$	$c_7O_7$	$d_1B_1$	$d_2B_2$				
$N_{\frac{1}{2}}^+$	1467	-8	32	36	19	0	-31	0	0	$1499 \pm 10$	$1538 \pm 18$	$S_{11}(1535)$ ****	
$\Lambda_{\frac{1}{2}}^+$								138	15	$1668 \pm 9$	$1670 \pm 10$	$S_{01}(1670)$ ****	
$\Sigma_{\frac{1}{2}}^+$								138	-25	$1628 \pm 10$			
$\Xi_{\frac{1}{2}}^+$								276	0	$1791 \pm 13$			
$N_{\frac{3}{2}}^+$	1467	4	32	36	-10	0	16	0	0	$1542 \pm 10$	$1523 \pm 8$	$D_{13}(1520)$ ****	
$\Lambda_{\frac{3}{2}}^+$								138	15	$1698 \pm 8$	$1690 \pm 5$	$D_{03}(1690)$ ****	
$\Sigma_{\frac{3}{2}}^+$								138	-25	$1658 \pm 9$	$1675 \pm 10$	$D_{13}(1670)$ ****	
$\Xi_{\frac{3}{2}}^+$								276	0	$1821 \pm 11$	$1823 \pm 5$	$D_{13}(1820)$ ***	
$N_{\frac{1}{2}}^{\prime}$	1467	-20	162	36	48	-18	42	0	0	$1648 \pm 11$	$1660 \pm 20$	$S_{11}(1650)$ ****	
$\Lambda_{\frac{1}{2}}^{\prime}$								138	15	$1784 \pm 16$	$1785 \pm 65$	$S_{01}(1800)$ ***	
$\Sigma_{\frac{1}{2}}^{\prime}$								138	-25	$1745 \pm 17$	$1765 \pm 35$	$S_{11}(1750)$ ***	
$\Xi_{\frac{1}{2}}^{\prime}$								276	0	$1907 \pm 20$			
$N_{\frac{3}{2}}^{\prime}$	1467	-8	162	36	19	15	-17	0	0	$1675 \pm 10$	$1700 \pm 50$	$D_{13}(1700)$ ***	
$\Lambda_{\frac{3}{2}}^{\prime}$								138	15	$1826 \pm 12$			
$\Sigma_{\frac{3}{2}}^{\prime}$								138	-25	$1787 \pm 13$			
$\Xi_{\frac{3}{2}}^{\prime}$								276	0	$1949 \pm 16$			
$N_{\frac{5}{2}}^+$	1467	12	162	36	-29	-4	25	0	0	$1669 \pm 10$	$1678 \pm 8$	$D_{15}(1675)$ ****	
$\Lambda_{\frac{5}{2}}^+$								138	15	$1822 \pm 10$	$1820 \pm 10$	$D_{05}(1830)$ ****	
$\Sigma_{\frac{5}{2}}^+$								138	-25	$1782 \pm 11$	$1775 \pm 5$	$D_{15}(1775)$ ****	
$\Xi_{\frac{5}{2}}^+$								276	0	$1945 \pm 14$			

	Part. contrib. (MeV)										Total (MeV)	Exp. (MeV)	Name, status
	$c_1 O_1$	$c_2 O_2$	$c_3 O_3$	$c_4 O_4$	$c_5 O_5$	$c_6 O_6$	$c_7 O_7$	$d_1 B_1$	$d_2 B_2$				
$\Delta_{\frac{1}{2}}$	1467	8	32	181	38	0	-24	0	0	1702 $\pm$ 18	1645 $\pm$ 30	$S_{31}(1620)^{****}$	
$\Sigma''_{\frac{1}{2}}$								138	34	1875 $\pm$ 16			
$\Xi''_{\frac{1}{2}}$								276	59	2037 $\pm$ 22			
$\Omega_{\frac{1}{2}}$								413	74	2190 $\pm$ 29			
$\Delta_{\frac{3}{2}}$	1467	-4	32	181	-19	0	12	0	0	1668 $\pm$ 20	1720 $\pm$ 50	$D_{33}(1700)^{****}$	
$\Sigma''_{\frac{3}{2}}$								138	34	1841 $\pm$ 16			
$\Xi''_{\frac{3}{2}}$								276	59	2003 $\pm$ 21			
$\Omega_{\frac{3}{2}}$								413	74	2156 $\pm$ 27			
$\Lambda''_{\frac{1}{2}}$	1467	-24	32	-108	0	0	-38	138	-44	1421 $\pm$ 14	1407 $\pm$ 4	$S_{01}(1405)^{****}$	
$\Lambda''_{\frac{3}{2}}$	1467	12	32	-108	0	0	19	138	-44	1515 $\pm$ 14	1520 $\pm$ 1	$D_{03}(1520)^{****}$	
$N_{1/2} - N'_{1/2}$	0	-8	0	0	-10	-55	18	0	0	-55			
$N_{3/2} - N'_{3/2}$	0	-12	0	0	-15	17	28	0	0	18			



## Status of $\Lambda(1405)$

- Negative parity baryon resonance with  $J = 1/2, I = 0, S = -1$
- Difficult to be described by **constituent quark models** (mass too large, small mass difference with spin-orbit partner ( $\Lambda(1520)$ ))
- Mass well described in the **first approach**,  $S_c = 0$  contributions  
⇒ **Vanishing Spin-Spin** contributions
- Not so well described in **our picture**,  $S_c = 1$  contributions also included  
⇒ **Nonvanishing Spin-Spin** contributions
- $\Lambda(1405)$ ,  $qqq$  state? Meson-Baryon “molecule” nature suggested by study of  $N_c$  dependence of decay widths [13]

[13] T. Hyodo, D. Jido, L. Roca, Phys. Rev. **D77**, 056010 (2008).

# Conclusions

- $[70, 1^-]$  baryon masses
- Two complementary approaches :
  - **Core + excited quark** ignores isospin terms
  - **Exact wave function** includes isospin term
    - ⇒ Contribution to  $\Delta$  similar to that of spin terms in  $N$
    - ⇒ Flavor dependent interactions are required
- Status of  $\Lambda(1405)$  still **uncertain**
  - ⇒ more studies in large  $N_c$
- Analysis of multiplets higher than  $[70, 1^-]$  is necessary (work in progress)